

**EX:** Find the polar form of  $2.5 - j3.2$ .

**ANS:**  $4.06e^{-j52^\circ}$

**SOL'N:** We express  $2.5 - j3.2$  in polar form  $Ae^{j\phi}$ .

Use the pythagorean theorem to find magnitude  $A$ :

$$A = \sqrt{2.5^2 + 3.2^2} \approx 4.06$$

Set the tangent of the phase angle equal to the side opposite (imaginary part) over the side adjacent (real part):

$$\tan \phi = \frac{\text{Im}[2.5 - j3.2]}{\text{Re}[2.5 - j3.2]} = \frac{-3.2}{2.5} = -1.28$$

$$\phi = \tan^{-1}\left(\frac{-3.2}{2.5}\right) \approx -52^\circ \text{ or } -0.9076 \text{ radians}$$

Our final answer:

$$2.5 - j3.2 \approx 4.06e^{-j52^\circ}$$

**NOTE:** When calculating the inverse tangent, if we use -1.28 rather than both the imaginary and real parts, we have two possible values for  $\phi$  that differ by 180 degrees. The ratio of the imaginary and real parts is the same for  $1 + j$  and  $-1 - j$ , for example. Thus, it is necessary to keep track of which quadrant the complex number lies in if we wish to avoid confusion about the correct value of phase angle  $\phi$ .