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|---|---|--|---|--|
| <b>UNIFORM DISTRIBUTION:</b><br>$X \sim u(0,1)$                     | $f(x) = \begin{cases} 1 & 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$  | $\mu = \frac{1}{2}$                        | $\sigma^2 = \frac{1}{12}$                                   |  |
| <b>GAUSSIAN (NORMAL) DISTRIBUTION:</b><br>$X \sim N(\mu, \sigma^2)$ | $f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-(x-\mu)^2/2\sigma^2}$   | $\mu$                                      | $\sigma^2$  | Standard gaussian has $\mu = 0$ and $\sigma^2 = 1$   |
| <b>EXPONENTIAL DISTRIBUTION:</b><br>$X \sim ex(\beta)$              | $f(x) = \begin{cases} \frac{1}{\beta} e^{-x/\beta} & x > 0 \\ 0 & \text{otherwise} \end{cases}$   | $\mu = \beta$                              | $\sigma^2 = \beta^2$  | $f(x)$ = gamma dist with $\alpha = 1$  |
| <b>GAMMA DISTRIBUTION:</b><br>$X \sim \gamma(\alpha, \beta)$        | $f(x) = \begin{cases} \frac{1}{\beta^\alpha \Gamma(\alpha)} x^{\alpha-1} e^{-x/\beta} & x > 0 \\ 0 & \text{otherwise} \end{cases}$      | $\mu = \alpha\beta$                        | $\sigma^2 = \alpha\beta^2$                                  | $f(x)$ = pdf for time of occurrence of $\alpha$ th event of Poisson proc with event rate $\lambda = 1/\beta$ |
| <b>LOGNORMAL DISTRIBUTION:</b><br>$X \sim \ln N(\mu_Y, \sigma_Y^2)$ | $f_X(x) = \begin{cases} \frac{1}{x\sqrt{2\pi\sigma_Y^2}} e^{-[\ln(x)-\mu_Y]^2/2\sigma_Y^2} & x > 0 \\ 0 & \text{otherwise} \end{cases}$ | $\mu_X = e^{\mu_Y + \frac{\sigma_Y^2}{2}}$ | $\sigma_X^2 = e^{2\mu_Y + \sigma_Y^2} (e^{\sigma_Y^2} - 1)$ | If $Y$ is gaussian distributed, then $X = e^Y$ is lognormal.   |
| <b>CHI-SQUARED DISTRIBUTION:</b><br>$X \sim \chi_n^2$               | $f(x) = \begin{cases} \frac{1}{2^{v/2}\Gamma(v/2)} x^{(v-2)/2} e^{-x/2} & x > 0 \\ 0 & \text{otherwise} \end{cases}$                    | $\mu = v$                                  | $\sigma^2 = 2v$   | Sum of $v$ standard gaussians squared is chi-squared of degree $v$ .   |