

**TOOL:**

|               | Inverse DTFT                                                                   | $\Longleftrightarrow$ | DTFT                                                                  |
|---------------|--------------------------------------------------------------------------------|-----------------------|-----------------------------------------------------------------------|
| Definition    | $x[n] = \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\omega}) e^{j\omega n} d\omega$ | $\Longleftrightarrow$ | $X(e^{j\omega}) \equiv \sum_{n=-\infty}^{\infty} x[n] e^{-j\omega n}$ |
|               | $x[n]$                                                                         | $\Longleftrightarrow$ | $X(e^{j\omega})$                                                      |
|               | $y[n]$                                                                         | $\Longleftrightarrow$ | $Y(e^{j\omega})$                                                      |
| Linearity     | $ax[n] + by[n]$                                                                | $\Longleftrightarrow$ | $aX(e^{j\omega}) + bY(e^{j\omega})$                                   |
| Conjugation   | $x^*[n]$                                                                       | $\Longleftrightarrow$ | $X^*(e^{-j\omega})$                                                   |
| Symmetry      | $x[n]$ real valued                                                             | $\Longleftrightarrow$ | $X(e^{j\omega}) = X^*(e^{-j\omega})$                                  |
| Time reversal | $x[-n]$                                                                        | $\Longleftrightarrow$ | $X(e^{-j\omega})$                                                     |
| Time shift    | $x[n-d]$                                                                       | $\Longleftrightarrow$ | $e^{-j\omega d} X(e^{j\omega})$                                       |
| Modulation    | $x[n] e^{j\omega_0 n}$                                                         | $\Longleftrightarrow$ | $X(e^{-j(\omega+\omega_0)})$                                          |
| Convolution   | $y[n] = x[n] * h[n]$                                                           | $\Longleftrightarrow$ | $Y(e^{j\omega}) = X(e^{j\omega}) H(e^{j\omega})$                      |
| Parseval's    | $\sum_{n=-\infty}^{\infty}  x[n] ^2$                                           | $=$                   | $\frac{1}{2\pi} \int_{-\pi}^{\pi}  X(e^{j\omega}) ^2 d\omega$         |

**REF:** Ronald Bracewell, *The Fourier Transform and its Applications*, 2nd Ed., New York, NY: McGraw-Hill, 1978. ISBN 0-07-007013-X

Alan V. Oppenheim and Alan S. Willsky, with S. Hamid Nawab, *Signals and Systems*, 2nd Edition, Upper Saddle River, NJ: Prentice Hall, 1996. ISBN 0-13-814757-4