

<b>STANDARD NORMAL</b> $Z = \frac{\bar{X} - \mu}{\sigma / \sqrt{n}}$	$f_Z(z) = \frac{1}{\sqrt{2\pi}} e^{-z^2/2}, \quad -\infty < z < \infty$	<b>SINGLE MEAN</b> $\sigma$ known data i.i.d. normal
<b>t-DISTRIBUTION</b> (v degrees freedom) $T = \frac{\bar{X} - \mu}{S / \sqrt{n}}$	$f_T(t) = \frac{\Gamma\left(\frac{v+1}{2}\right)}{\Gamma\left(\frac{v}{2}\right)\sqrt{\pi v}} \left(1 + \frac{t^2}{v}\right)^{-(v+1)/2}, \quad -\infty < t < \infty$	<b>SINGLE MEAN</b> $\sigma$ unknown $v \equiv n - 1$ data i.i.d. normal
<b>STANDARD NORMAL</b> $Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}}$	$f_Z(z) = \frac{1}{\sqrt{2\pi}} e^{-z^2/2}, \quad -\infty < z < \infty$	<b>TWO MEANS</b> $\sigma$ 's known data i.i.d. normal
<b>t-DISTRIBUTION (APPROX)</b> (v degrees freedom) $T' = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$	$f_T(t) \approx \frac{\Gamma\left(\frac{v+1}{2}\right)}{\Gamma\left(\frac{v}{2}\right)\sqrt{\pi v}} \left(1 + \frac{t^2}{v}\right)^{-(v+1)/2}, \quad -\infty < t < \infty$	<b>TWO MEANS</b> $\sigma$ 's unknown $v = \frac{(s_1^2/n_1 + s_2^2/n_2)^2}{\left(\frac{s_1^2}{n_1}\right)^2 + \left(\frac{s_2^2}{n_2}\right)^2}$ $n_1 - 1 \quad n_2 - 1$ data i.i.d. normal, distribution is approx
<b><math>\chi^2</math>-DISTRIBUTION</b> (v degrees freedom) $X^2 = \frac{(n-1)S^2}{\sigma^2}$	$f_{X^2}(\chi) = \begin{cases} \frac{1}{2^{v/2}\Gamma\left(\frac{v}{2}\right)} \frac{\chi^{(v-1)/2}}{\sqrt{\chi}} e^{-\chi/2}, & \chi > 0 \\ 0 & \chi \leq 0 \end{cases}$	<b>ONE VARIANCE</b> $\sigma$ known $v \equiv n - 1$ data i.i.d. normal
<b>F-DISTRIBUTION</b> (v <sub>1</sub> , v <sub>2</sub> degrees freedom) $F = \frac{S_1^2/\sigma_1^2}{S_2^2/\sigma_2^2}$	$f_F(f) = \begin{cases} \frac{\Gamma\left(\frac{v_1+v_2}{2}\right)\left(\frac{v_1}{v_2}\right)^{\frac{v_1}{2}} f^{\frac{v_1}{2}}}{\Gamma\left(\frac{v_1}{2}\right)\Gamma\left(\frac{v_2}{2}\right)\left(1 + \frac{v_1 f}{v_2}\right)^{\frac{v_1+v_2}{2}}}, & f > 0 \\ 0 & f \leq 0 \end{cases}$	<b>TWO VARIANCES</b> $\sigma$ 's unknown $v_1 \equiv n_1 - 1$ $v_2 \equiv n_2 - 1$ data i.i.d. normal

**REF:** [1] Ronald E. Walpole, Raymond H. Myers, Sharon L. Myers, and Keying Ye, *Probability and Statistics for Engineers and Scientists*, 8th Ed., Upper Saddle River, NJ: Prentice Hall, 2007.